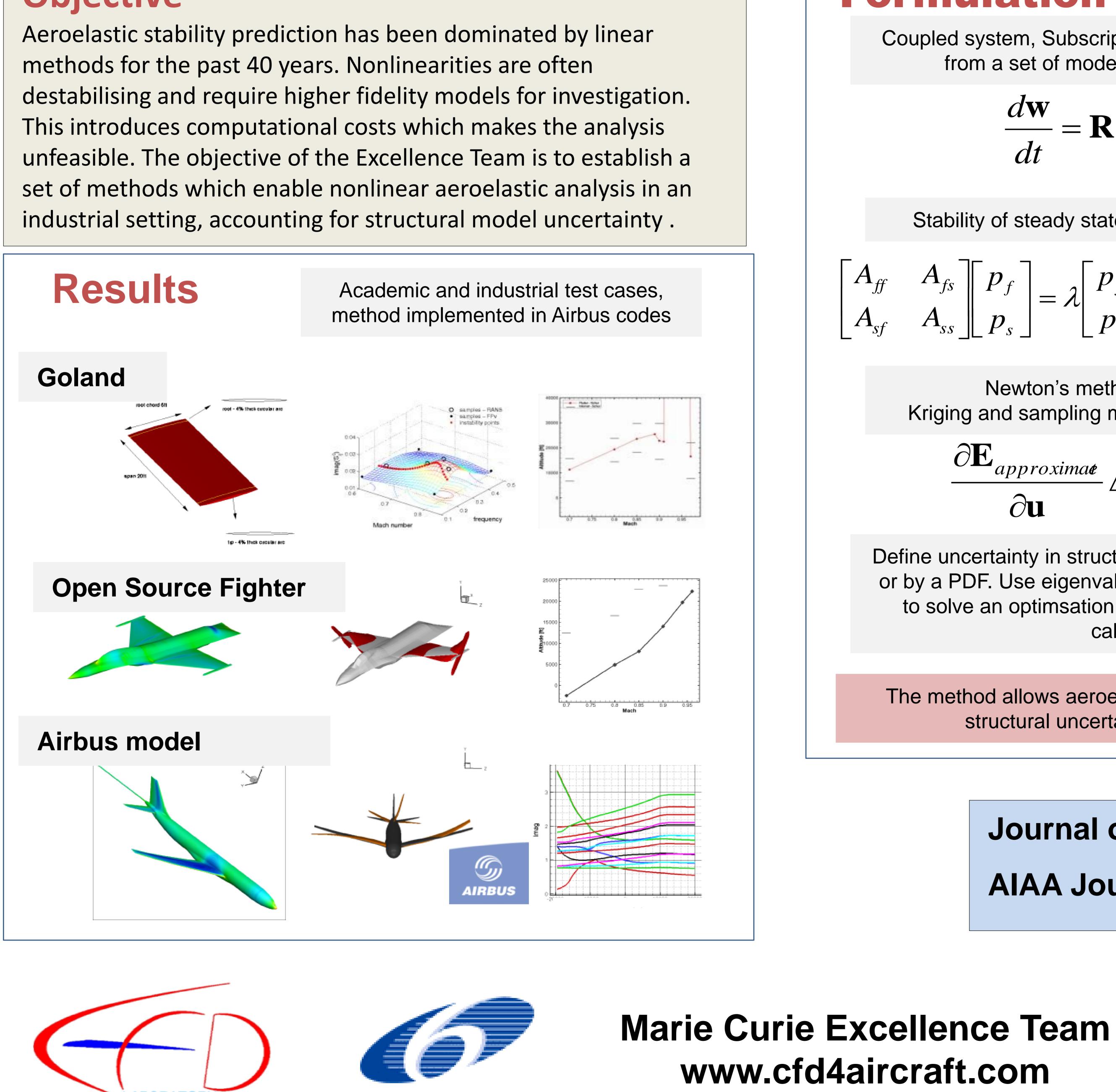
Enabling Aeroelastic Certification by Analysis K.J.Badcock, S.Timme, S.Marques, H.Khodaparast, M.Prandina, J.E.Mottershead

Objective



Formulation

Coupled system, Subscripts f=fluid, s=structure; fluid model from CFD, structural model from a set of modes, typical dimension for aircraft models 10 millions DoF

$$\frac{d\mathbf{w}}{dt} = \mathbf{R}(\mathbf{w}, \mu) \qquad \mathbf{w} = \begin{bmatrix} \mathbf{w}_f \\ \mathbf{w}_s \end{bmatrix} \qquad \mathbf{I}$$

Stability of steady state from eigenvalue problem, dimension of E – order 10-100

$$\begin{bmatrix} p_f \\ p_s \end{bmatrix} = \lambda \begin{bmatrix} p_f \\ p_s \end{bmatrix} \longrightarrow \begin{bmatrix} E = S(\lambda) p_s - \lambda \\ S(\lambda) = (A_{ss} - \lambda) \end{bmatrix}$$

Newton's method is used to solve small order nonlinear system E=0 Kriging and sampling methods approximate $S(\lambda, M, altitude)$ for approximate Jacobian

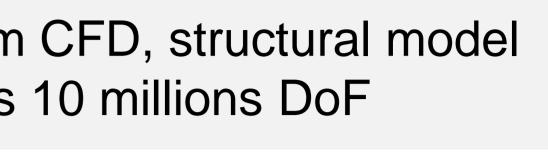
$$\frac{\partial \mathbf{E}_{approximat}}{\partial \mathbf{u}} \Delta \mathbf{u} = -\mathbf{E} \qquad \mathbf{u} = [\mathbf{p}_s, \lambda]$$

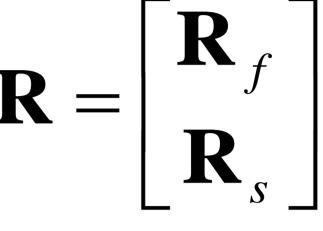
Define uncertainty in structure by a set of modes arising from parameters defined in intervals or by a PDF. Use eigenvalue solver to calculate realisations for a Monte Carlo simulation or to solve an optimsation problem for the interval problem. The approximate Jacobian is calculated once at a nominal structural state.

The method allows aeroelastic stability searches over the flight envelope in the presence of structural uncertainty using high fidelity models accounting for nonlinearity

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- $p_{c} = 0$

 $U - A_{sf} (A_{ff} - \lambda I)^{-1} A_{fs}$

